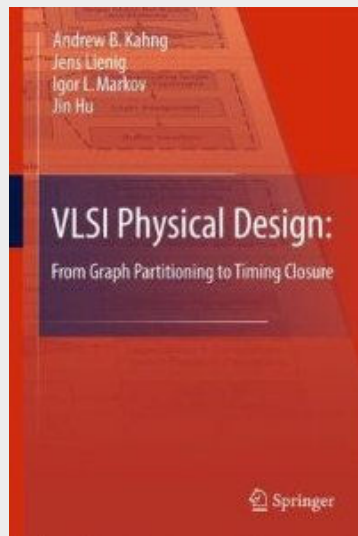


# *VLSI Physical Design: From Graph Partitioning to Timing Closure*

## **Chapter 7 – Specialized Routing**

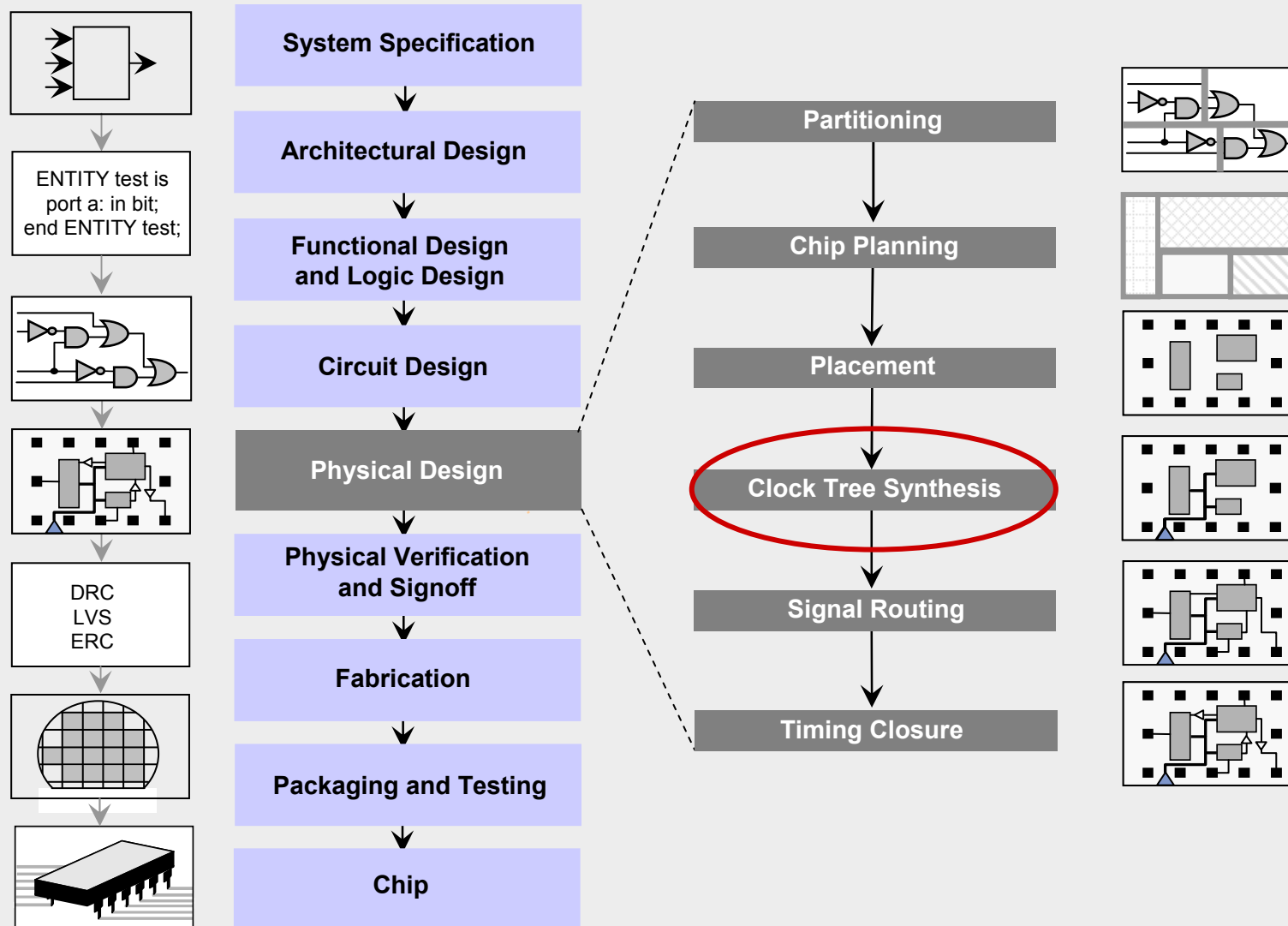


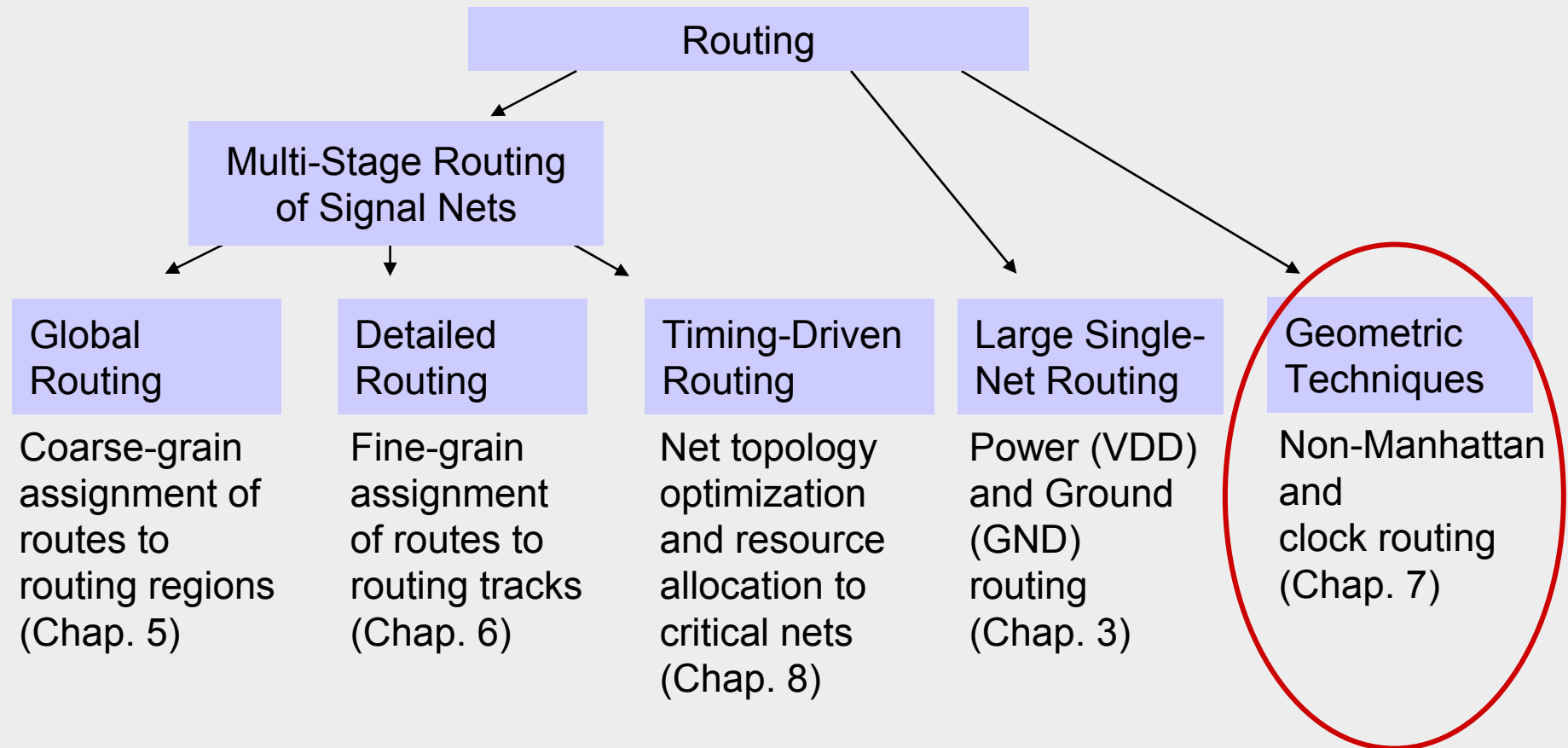
Original Authors:

Andrew B. Kahng, Jens Lienig, Igor L. Markov, Jin Hu

## Chapter 7 – Specialized Routing

- 7.1 Introduction to Area Routing
- 7.2 Net Ordering in Area Routing
- 7.3 Non-Manhattan Routing
  - 7.3.1 Octilinear Steiner Trees
  - 7.3.2 Octilinear Maze Search
- 7.4 Basic Concepts in Clock Networks
  - 7.4.1 Terminology
  - 7.4.2 Problem Formulations for Clock-Tree Routing
- 7.5 Modern Clock Tree Synthesis
  - 7.5.1 Constructing Trees with Zero Global Skew
  - 7.5.2 Clock Tree Buffering in the Presence of Variation





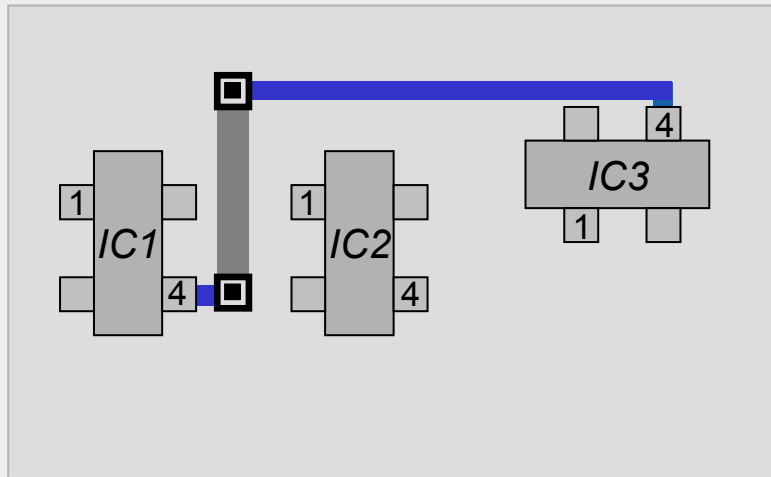
- **Area routing** directly constructs metal routes for signal connections (no global and detailed routing, Secs. 7.1-7.2)
- **Non-Manhattan routing** is presented in Sec. 7.3
- **Clock signals** and other nets that require special treatment are discussed in Secs. 7.4-7.5

## 7.1 Introduction to Area Routing

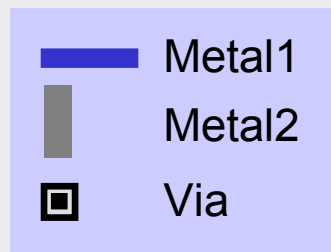
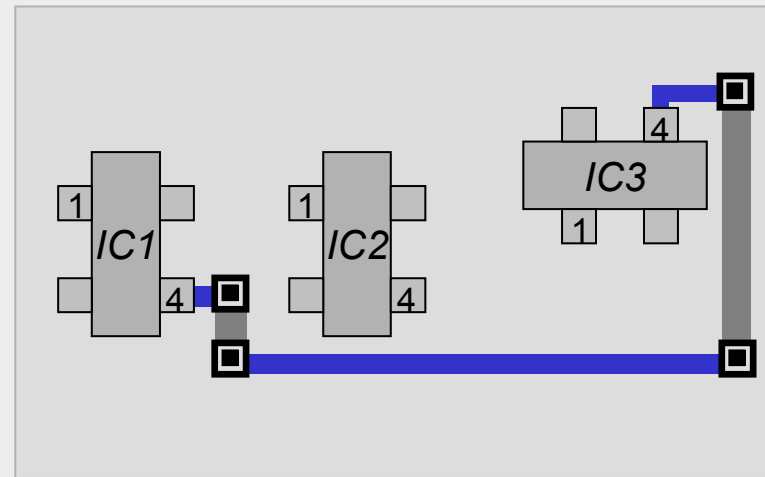
- The goal of area routing is to route all nets in the design
  - without global routing
  - within the given layout space
  - while meeting all geometric and electrical design rules
- Area routing performs the following optimizations
  - minimizing the total routed length and number of vias of all nets
  - minimizing the total area of wiring and the number of routing layers
  - minimizing the circuit delay and ensuring an even wire density
  - avoiding harmful capacitive coupling between neighboring routes
- Subject to
  - technology constraints (number of routing layers, minimal wire width, etc.)
  - electrical constraints (signal integrity, coupling, etc.)
  - geometry constraints (preferred routing directions, wire pitch, etc.)

## 7.1 Introduction to Area Routing

Minimal wirelength:



Alternative routing path:

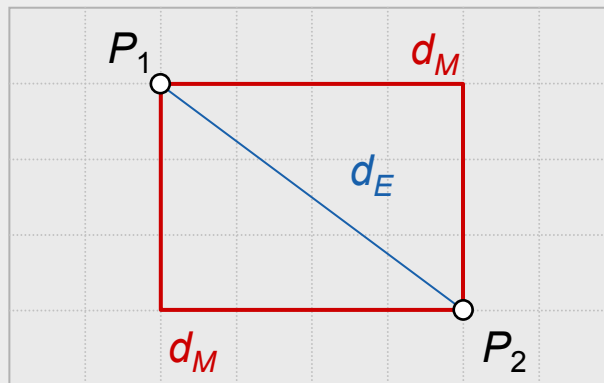


## 7.1 Introduction to Area Routing

Distance metric between two points  $P_1(x_1, y_1)$  and  $P_2(x_2, y_2)$

Euclidean distance  $d_E(P_1, P_2) = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} = \sqrt{(\Delta x)^2 + (\Delta y)^2}$

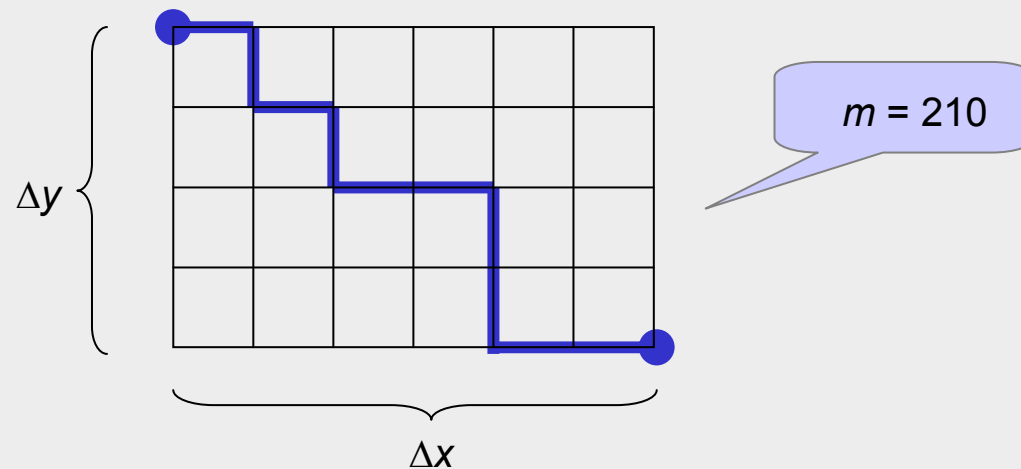
Manhattan distance  $d_M(P_1, P_2) = |x_2 - x_1| + |y_2 - y_1| = |\Delta x| + |\Delta y|$





## 7.1 Introduction to Area Routing

- Multiple Manhattan shortest paths between two points

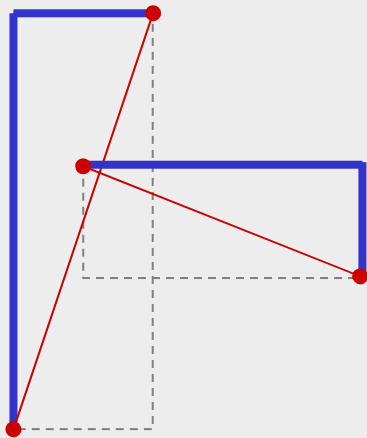


With no obstacles, the number of Manhattan shortest paths in an  $\Delta x \times \Delta y$  region is

$$m = \binom{\Delta x + \Delta y}{\Delta x} = \binom{\Delta x + \Delta y}{\Delta y} = \frac{(\Delta x + \Delta y)!}{\Delta x! \Delta y!}$$

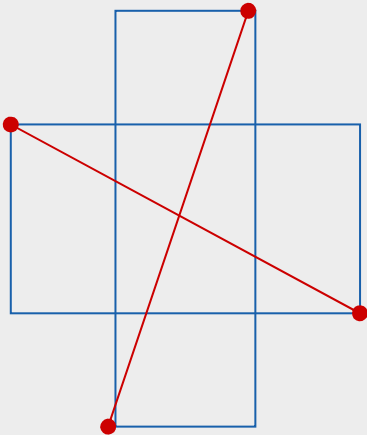
## 7.1 Introduction to Area Routing

- Two pairs of points may admit non-intersecting **Manhattan shortest paths**, while their **Euclidean shortest paths** intersect (but not vice versa).



## 7.1 Introduction to Area Routing

- If all pairs of **Manhattan shortest paths** between two pairs of points intersect, then so do **Euclidean shortest paths**.



## 7.1 Introduction to Area Routing

- The **Manhattan distance**  $d_M$  is (slightly) larger than the **Euclidean distance**  $d_E$ :

$$\frac{d_M}{d_E} = \begin{cases} 1.41 & \text{worst case: a square where } \Delta x = \Delta y \\ 1.27 & \text{on average, without obstacles} \\ 1.15 & \text{on average, with obstacles} \end{cases}$$

## 7.2 Net Ordering in Area Routing

7.1 Introduction to Area Routing

→ 7.2 Net Ordering in Area Routing

7.3 Non-Manhattan Routing

7.3.1 Octilinear Steiner Trees

7.3.2 Octilinear Maze Search

7.4 Basic Concepts in Clock Networks

7.4.1 Terminology

7.4.2 Problem Formulations for Clock-Tree Routing

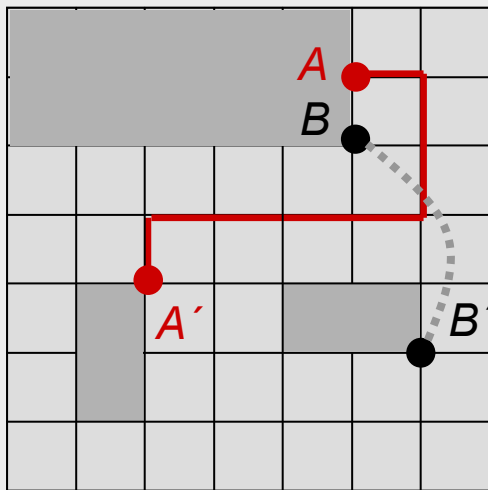
7.5 Modern Clock Tree Synthesis

7.5.1 Constructing Trees with Zero Global Skew

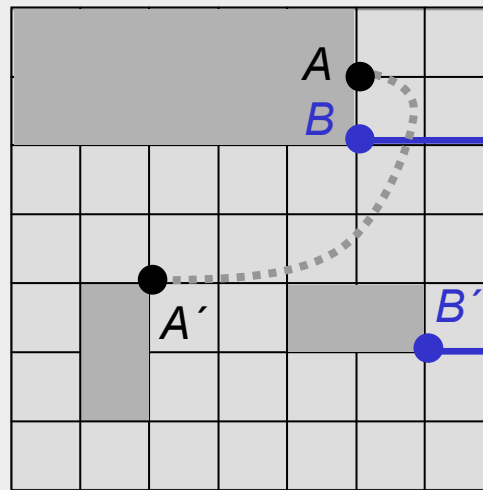
7.5.2 Clock Tree Buffering in the Presence of Variation

## 7.2 Net Ordering in Area Routing

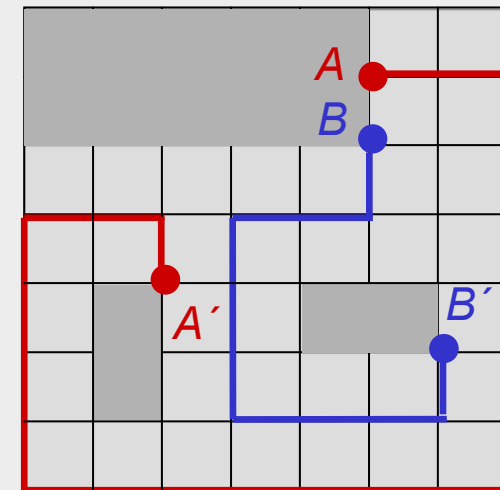
Effect of net ordering on routability



Optimal routing of net *A*



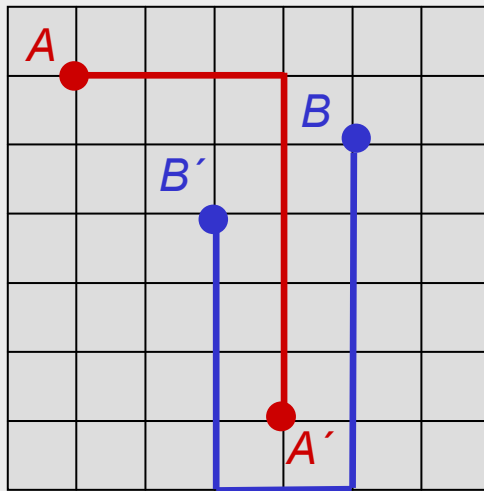
Optimal routing of net *B*



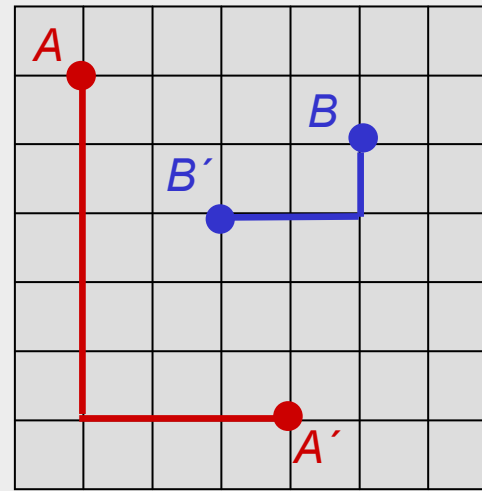
Nets *A* and *B* can be routed only with detours

## 7.2 Net Ordering in Area Routing

Effect of net ordering on total wirelength



Routing net *A* first



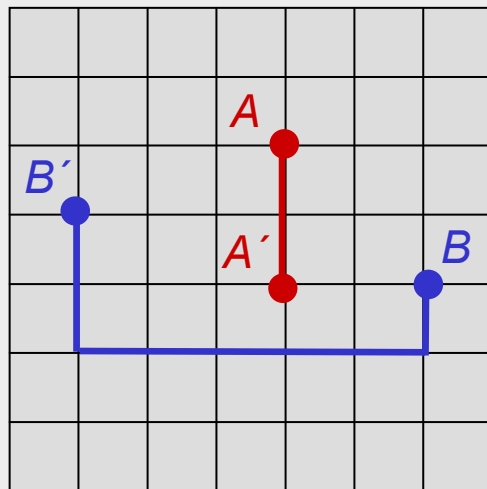
Routing net *B* first

## 7.2 Net Ordering in Area Routing

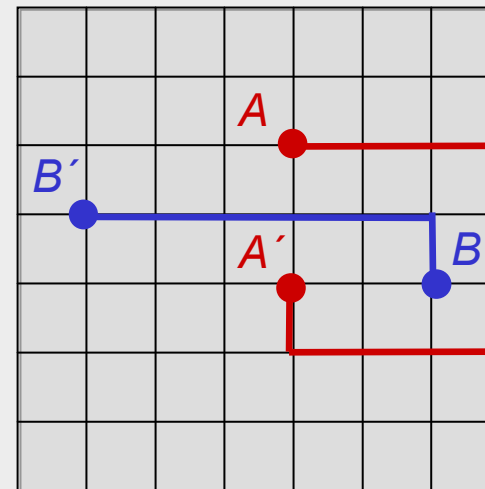
- For  $n$  nets, there are  $n!$  possible net orderings
- ⇒ Constructive heuristics are used

## 7.2 Net Ordering in Area Routing

- **Rule 1:** For two nets  $i$  and  $j$ , if *aspect ratio* ( $i$ ) > *aspect ratio* ( $j$ ), then  $i$  is routed before  $j$



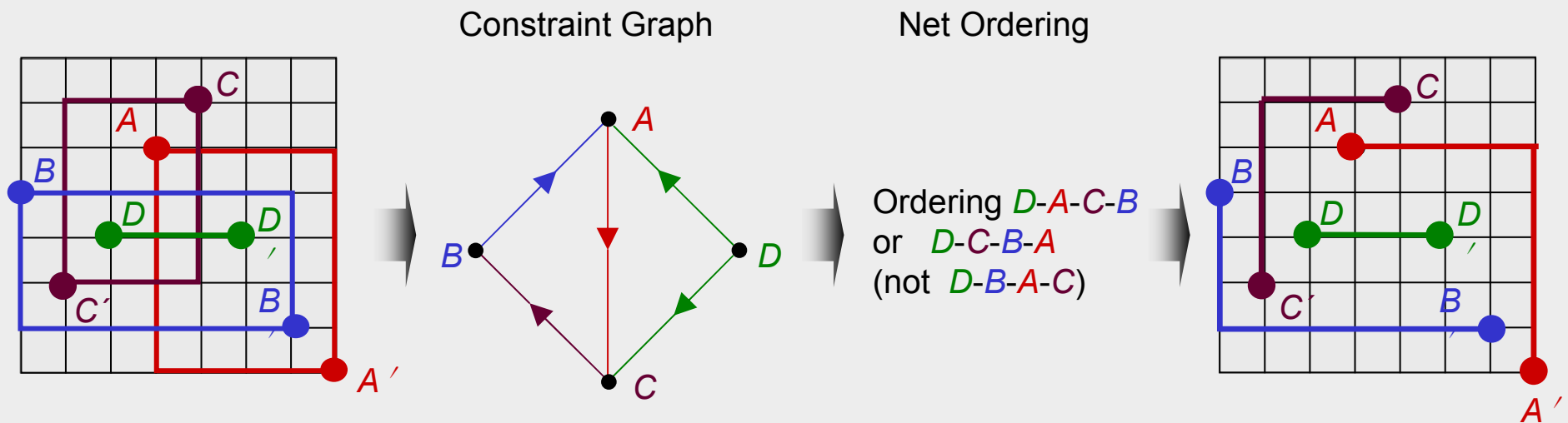
Net  $A$  has a higher aspect ratio of its bounding box; routing  $A$  first results in shorter total wirelength



Routing net  $B$  first results in longer total wirelength

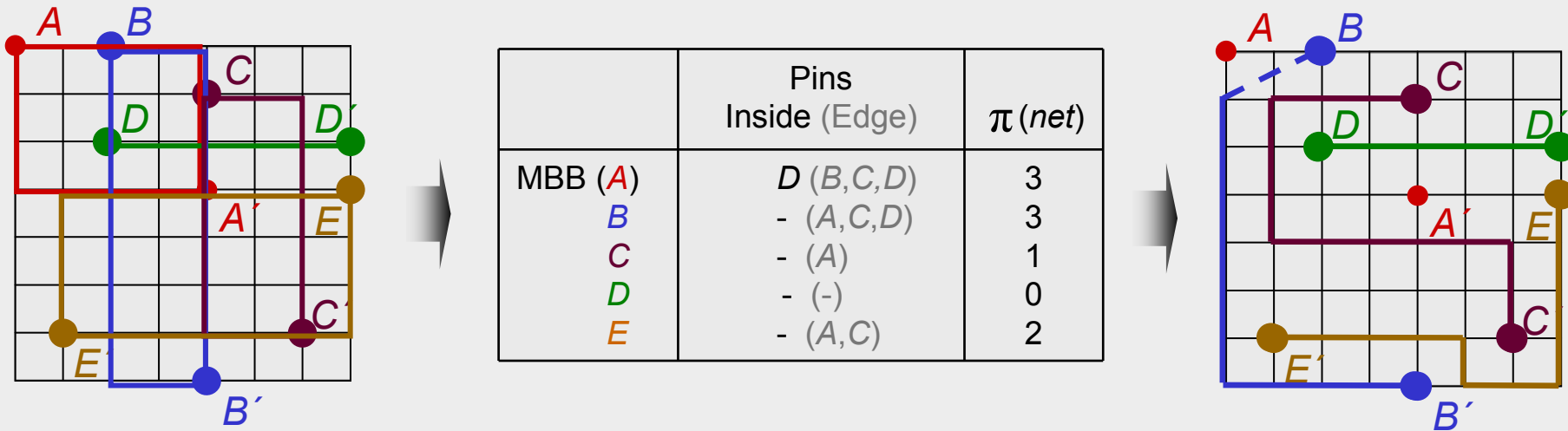
## 7.2 Net Ordering in Area Routing

- Rule 2:** For two nets  $i$  and  $j$ , if the pins of  $i$  are contained within  $MBB(j)$ , then  $i$  is routed before  $j$



## 7.2 Net Ordering in Area Routing

- Rule 3:** Let  $\Pi(net)$  be the number of pins within  $MBB(net)$  for net  $net$ . For two nets  $i$  and  $j$ , if  $\Pi(i) < \Pi(j)$ , then  $i$  is routed before  $j$ .
  - For each net, consider the pins of other nets within its bounding box
  - The net with the smallest number of such pins is routed first
  - Ties are broken based on the number of pins that are contained within the bounding box and on its edge



## 7.3 Non-Manhattan Routing

7.1 Introduction to Area Routing

7.2 Net Ordering in Area Routing

 7.3 Non-Manhattan Routing

7.3.1 Octilinear Steiner Trees

7.3.2 Octilinear Maze Search

7.4 Basic Concepts in Clock Networks

7.4.1 Terminology

7.4.2 Problem Formulations for Clock-Tree Routing

7.5 Modern Clock Tree Synthesis

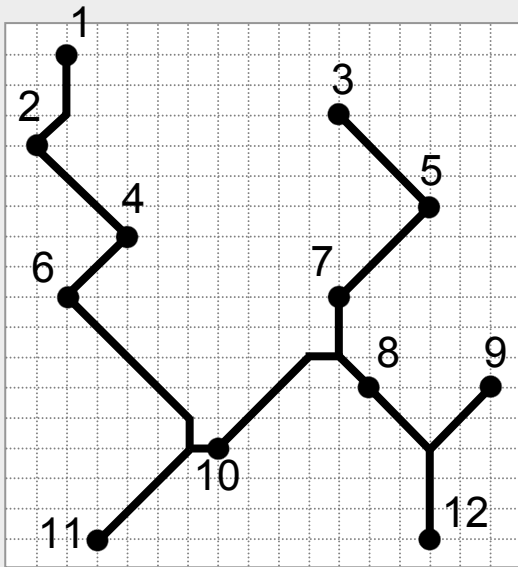
7.5.1 Constructing Trees with Zero Global Skew

7.5.2 Clock Tree Buffering in the Presence of Variation



## 7.3.1 Octilinear Steiner Trees

- Route planning using octilinear Steiner minimum trees (OSMT)
- Generalize rectilinear Steiner trees by allowing segments that extend in eight directions
- More freedom when placing Steiner points



## 7.3.1 Octilinear Steiner Trees

### Octilinear Steiner Tree Algorithm

**Input:** set of all pins  $P$  and their coordinates

**Output:** heuristic octilinear minimum Steiner tree  $OST$

$OST = \emptyset$

$T$  = set of all three-pin nets of  $P$  found by Delaunay triangulation

$sortedT$  = SORT( $T$ , minimum octilinear distance)

**for** ( $i = 1$  to  $|sortedT|$ )

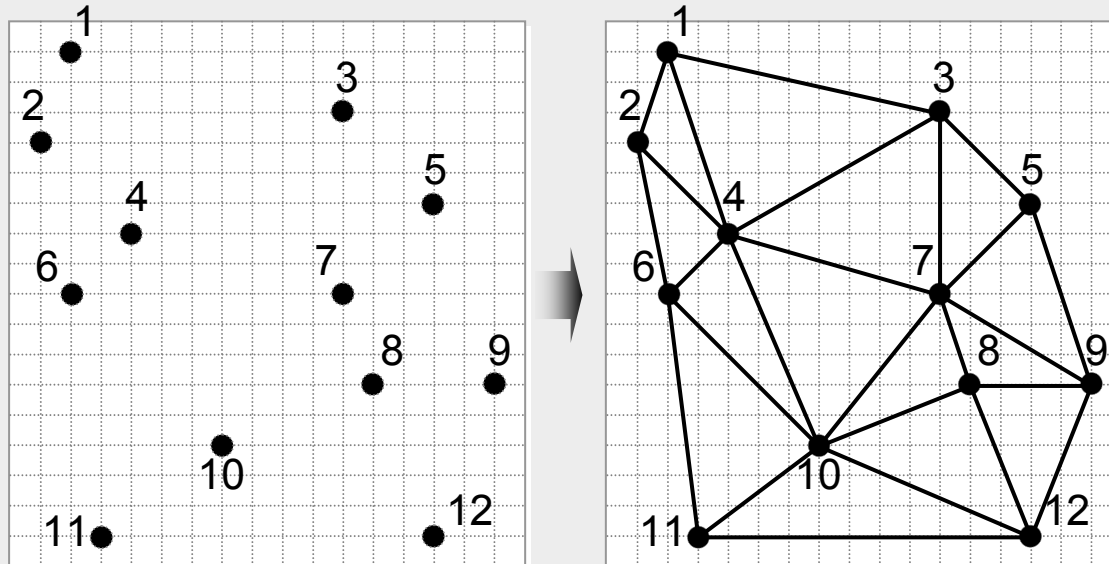
$subT$  = ROUTE( $sortedT[i]$ )      // route minimum tree over  $subT$

    ADD( $OST, subT$ )      // add route to existing tree

    IMPROVE( $OST, subT$ )      // locally improve  $OST$  based on  $subT$

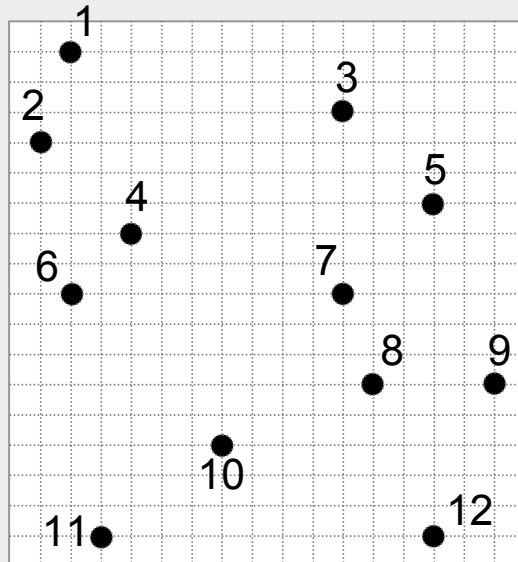
## 7.3.1 Octilinear Steiner Trees

(1) Triangulate

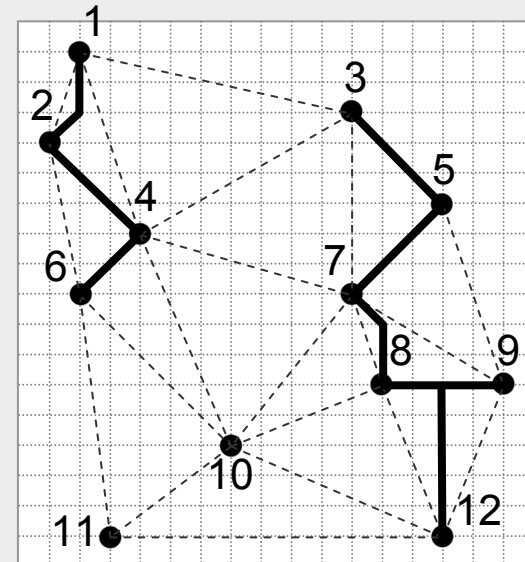
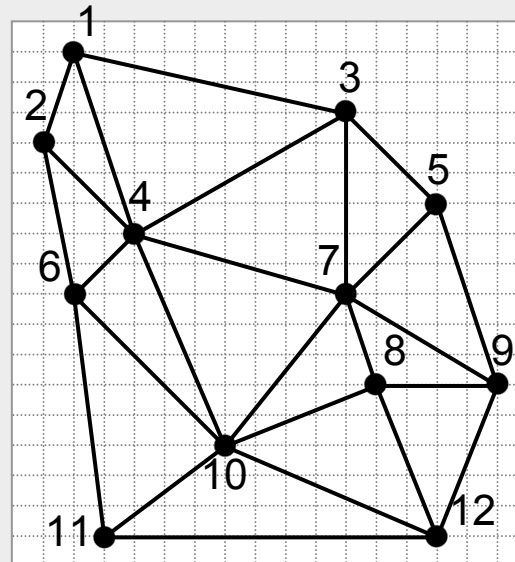


## 7.3.1 Octilinear Steiner Trees

(1) Triangulate

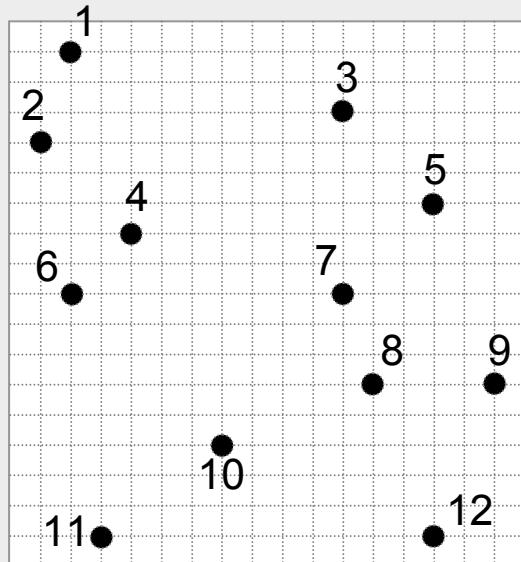


(2) Add route to existing tree

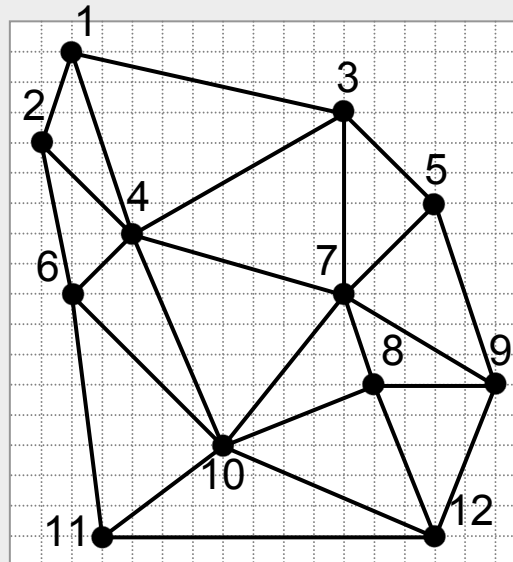


## 7.3.1 Octilinear Steiner Trees

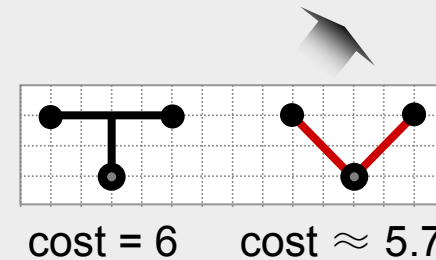
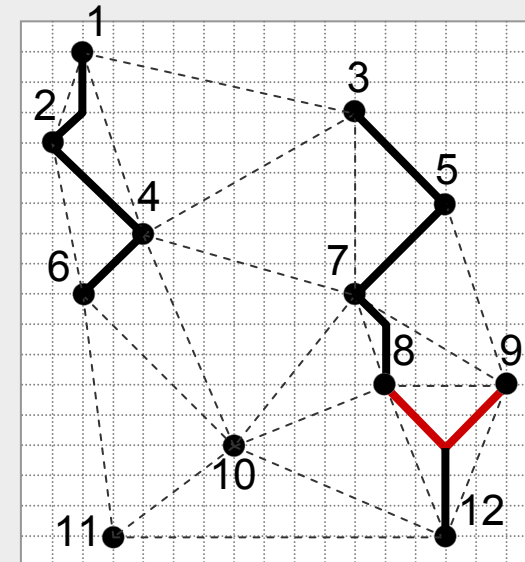
(1) Triangulate



(2) Add route to existing tree

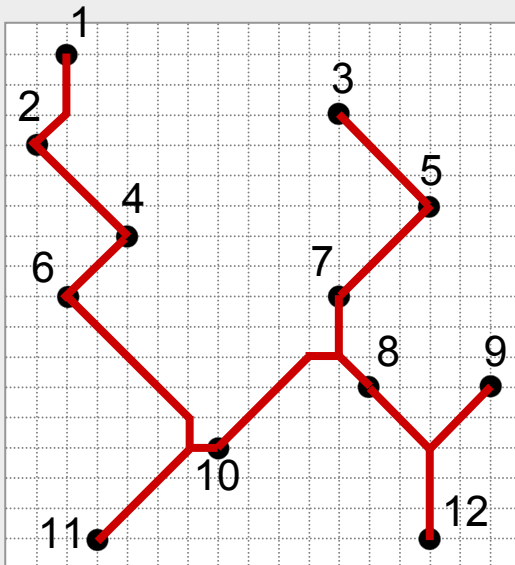


(3) Locally improve OST

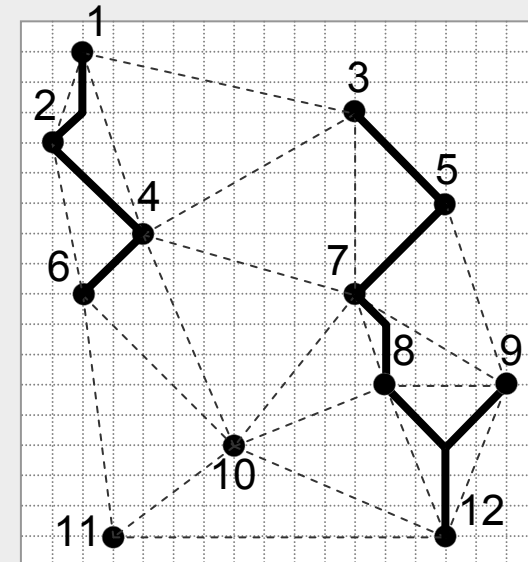


## 7.3.1 Octilinear Steiner Trees

Final OST after merging all subtrees

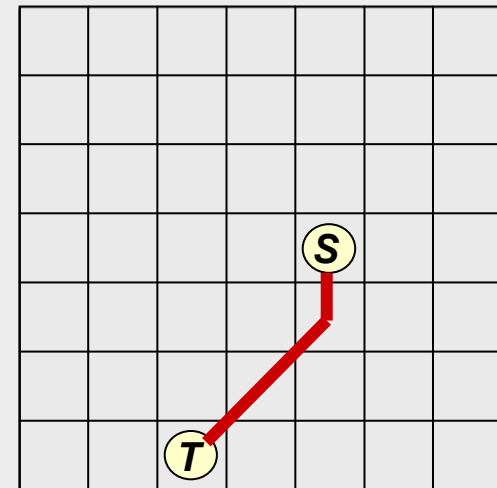


(3) Locally improve OST





## 7.3.2 Octilinear Maze Search



## 7.4 Basic Concepts in Clock Networks

7.1 Introduction to Area Routing

7.2 Net Ordering in Area Routing

7.3 Non-Manhattan Routing

7.3.1 Octilinear Steiner Trees

7.3.2 Octilinear Maze Search

 7.4 Basic Concepts in Clock Networks

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7.4.2 Problem Formulations for Clock-Tree Routing

7.5 Modern Clock Tree Synthesis

7.5.1 Constructing Trees with Zero Global Skew

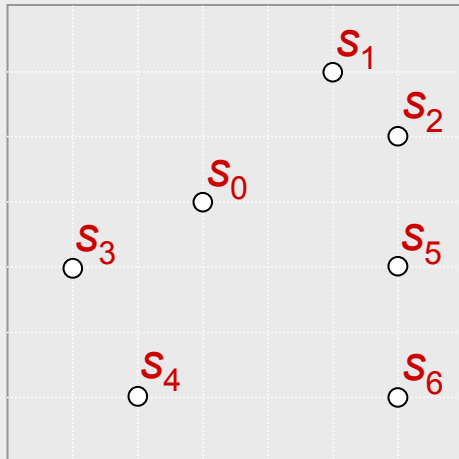
7.5.2 Clock Tree Buffering in the Presence of Variation

## 7.4.1 Terminology

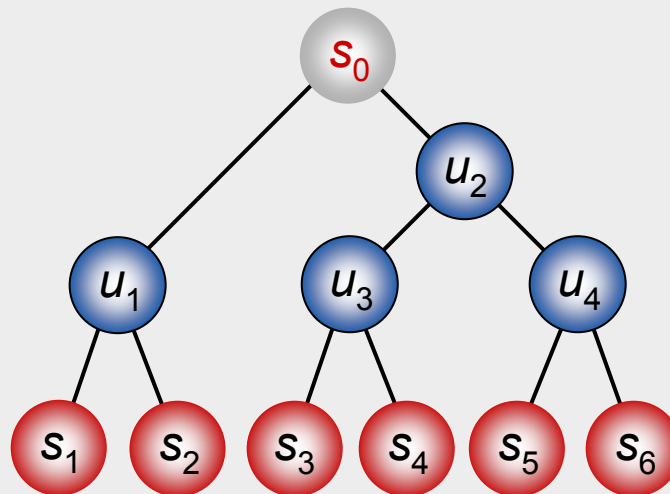
- A **clock routing instance (clock net)** is represented by  $n+1$  terminals, where  $s_0$  is designated as the source, and  $S = \{s_1, s_2, \dots, s_n\}$  is designated as sinks
  - Let  $s_i$ ,  $0 \leq i \leq n$ , denote both a terminal and its location
- A **clock routing solution** consists of a set of wire segments that connect all terminals of the clock net, so that a signal generated at the source propagates to all of the sinks
  - Two aspects of clock routing solution: topology and geometric embedding
- The **clock-tree topology (clock tree)** is a rooted binary tree  $G$  with  $n$  leaves corresponding to the set of sinks
  - Internal nodes = Steiner points

## 7.4.1 Terminology

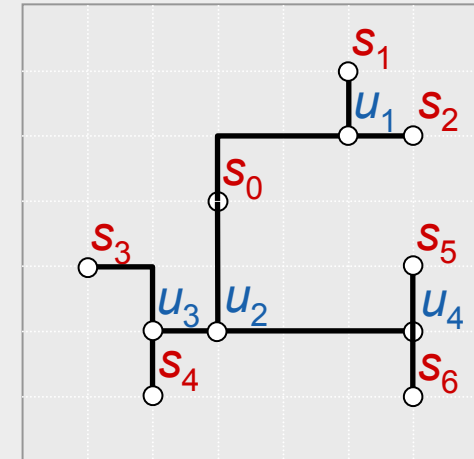
Clock routing  
problem instance



Connection topology



Embedding



## 7.4.1 Terminology

- Clock **skew**: (maximum) difference in clock signal arrival times between sinks

$$skew(T) = \max_{s_i, s_j \in S} |t(s_0, s_i) - t(s_0, s_j)|$$

- **Local skew**: maximum difference in arrival times of the clock signal at the clock pins of two or more related sinks
  - Sinks within distance  $d > 0$
  - Flip-flops or latches connected by a directed signal path
- **Global skew**: maximum difference in arrival times of the clock signal at the clock pins of any two (related or unrelated) sinks
  - Difference between shortest and longest source-sink path delays in the clock distribution network
  - The term “skew” typically refers to “global skew”

## 7.4.2 Problem Formulations for Clock-Tree Routing

- **Zero skew:** zero-skew tree (ZST)
  - ZST problem
- **Bounded skew:** true ZST may not be necessary in practice
  - Signoff timing analysis is sufficient with a non-zero skew bound
  - In addition to final (signoff) timing, this relaxation can be useful with intermediate delay models when it facilitates reductions in the length of the tree
  - Bounded-Skew Tree (BST) problem
- **Useful skew:** correct chip timing only requires control of the local skews between pairs of interconnected flip-flops or latches
  - Useful skew formulation is based on analysis of local skew constraints

## 7.5 Modern Clock Tree Synthesis

7.1 Introduction to Area Routing

7.2 Net Ordering in Area Routing

7.3 Non-Manhattan Routing

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7.3.2 Octilinear Maze Search

7.4 Basic Concepts in Clock Networks

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 7.5 Modern Clock Tree Synthesis

7.5.1 Constructing Trees with Zero Global Skew

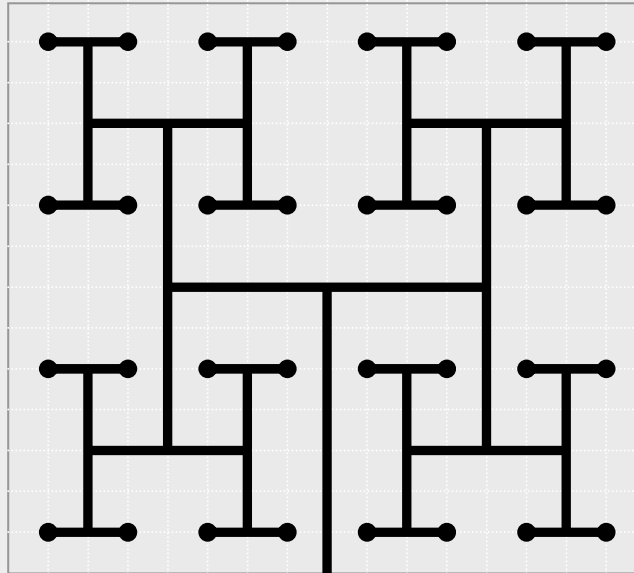
7.5.2 Clock Tree Buffering in the Presence of Variation

## 7.5 Modern Clock Tree Synthesis

- A clock tree should have low skew, while delivering the same signal to every sequential gate
- Clock tree synthesis is performed in two steps:
  - (1) Initial tree construction (Sec. 7.5.1) with one of these scenarios
    - Construct a regular clock tree, largely independent of sink locations
    - Simultaneously determine a topology and an embedding
    - Construct only the embedding, given a clock-tree topology as input
  - (2) Clock buffer insertion and several subsequent skew optimizations (Sec. 7.5.2)

## 7.5.1 Constructing Trees with Zero Global Skew

### H-tree



- Exact zero skew due to the symmetry of the H-tree
- Used for top-level clock distribution, not for the entire clock tree
  - Blockages can spoil the symmetry of an H-tree
  - Non-uniform sink locations and varying sink capacitances also complicate the design of H-trees

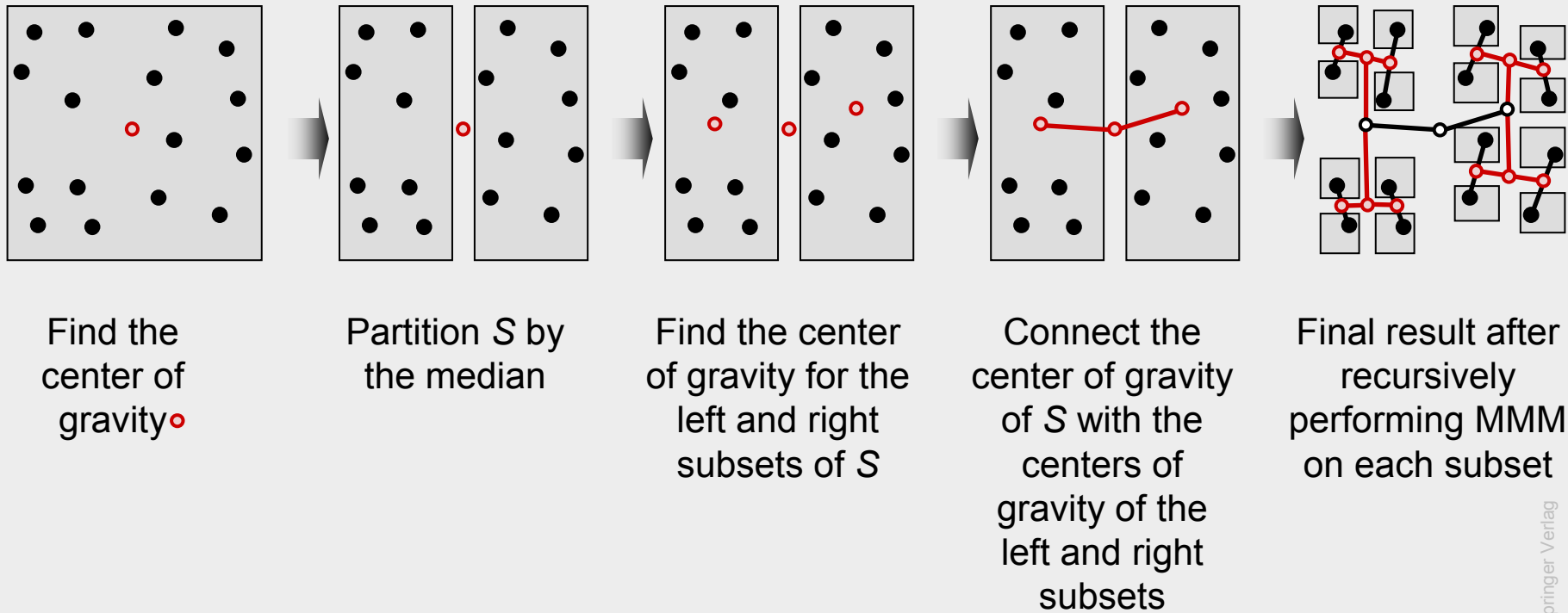
## 7.5.1 Constructing Trees with Zero Global Skew

### Method of Means and Medians (MMM)

- Can deal with arbitrary locations of clock sinks
- Basic idea:
  - Recursively partition the set of terminals into two subsets of equal size (median)
  - Connect the center of gravity (COG) of the set to the centers of gravity of the two subsets (the mean)

## 7.5.1 Constructing Trees with Zero Global Skew

### Method of Means and Medians (MMM)



## 7.5.1 Constructing Trees with Zero Global Skew

### Method of Means and Medians (MMM)

**Input:** set of sinks  $S$ , empty tree  $T$

**Output:** clock tree  $T$

**if** ( $|S| \leq 1$ )

**return**

```
( $x_0, y_0$ ) = ( $x_c(S), y_c(S)$ )           // center of mass for  $S$ 
( $S_A, S_B$ ) = PARTITION( $S$ )              // median to determine  $S_A$  and  $S_B$ 
( $x_A, y_A$ ) = ( $x_c(S_A), y_c(S_A)$ )     // center of mass for  $S_A$ 
( $x_B, y_B$ ) = ( $x_c(S_B), y_c(S_B)$ )     // center of mass for  $S_B$ 
ROUTE( $T, x_0, y_0, x_A, y_A$ )           // connect center of mass of  $S$  to
ROUTE( $T, x_0, y_0, x_B, y_B$ )           // center of mass of  $S_A$  and  $S_B$ 
BASIC_MMM( $S_A, T$ )                     // recursively route  $S_A$ 
BASIC_MMM( $S_B, T$ )                     // recursively route  $S_B$ 
```

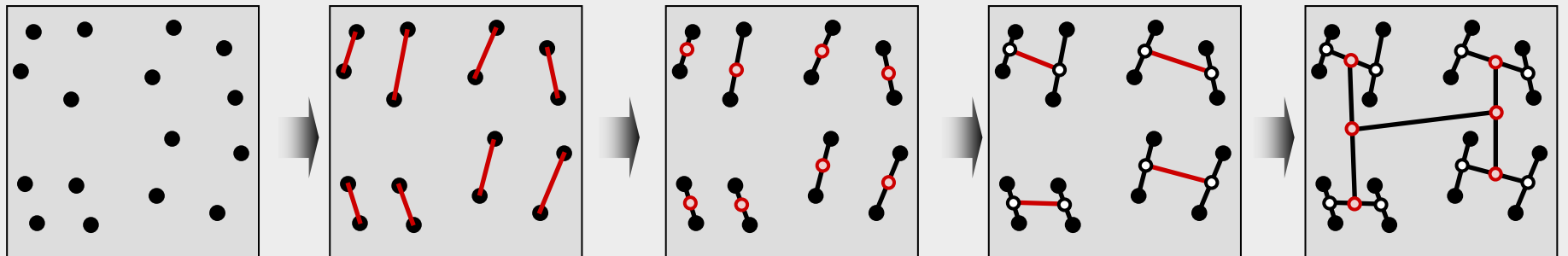
## 7.5.1 Constructing Trees with Zero Global Skew

### Recursive Geometric Matching (RGM)

- RGM proceeds in a bottom-up fashion
  - Compare to MMM, which is a top-down algorithm
- Basic idea:
  - Recursively determine a minimum-cost geometric matching of  $n$  sinks
  - Find a set of  $n / 2$  line segments that match  $n$  endpoints and minimize total length (subject to the matching constraint)
  - After each matching step, a balance or tapping point is found on each matching segment to preserve zero skew to the associated sinks
  - The set of  $n / 2$  tapping points then forms the input to the next matching step

## 7.5.1 Constructing Trees with Zero Global Skew

### Recursive Geometric Matching (RGM)



Set of  $n$   
sinks  $S$

Min-cost  
geometric  
matching

Find balance or  
tapping points  
(point that achieves  
zero skew in the  
subtree, not always  
midpoint)

Min-cost  
geometric  
matching

Final result after  
recursively  
performing RGM  
on each subset

## 7.5.1 Constructing Trees with Zero Global Skew

### Recursive Geometric Matching (RGM)

**Input:** set of sinks  $S$ , empty tree  $T$

**Output:** clock tree  $T$

**if** ( $|S| \leq 1$ )

**return**

$M$  = min-cost geometric matching over  $S$

$S' = \emptyset$

**foreach** ( $\langle P_i, P_j \rangle \in M$ )

$TP_i$  = subtree of  $T$  rooted at  $P_i$

$TP_j$  = subtree of  $T$  rooted at  $P_j$

$tp$  = tapping point on  $(P_i, P_j)$

    // point that minimizes the skew of

    // the tree  $T_{tp} = TP_i \cup TP_j \cup (P_i, P_j)$

    // add  $tp$  to  $S'$

    ADD( $S', tp$ )

    ADD( $T, (P_i, P_j)$ )

    // add matching segment  $(P_i, P_j)$  to  $T$

**if** ( $|S| \% 2 == 1$ )

    // if  $|S|$  is odd, add unmatched node

    ADD( $S'$ , unmatched node)

RGM( $S', T$ )

    // recursively call RGM

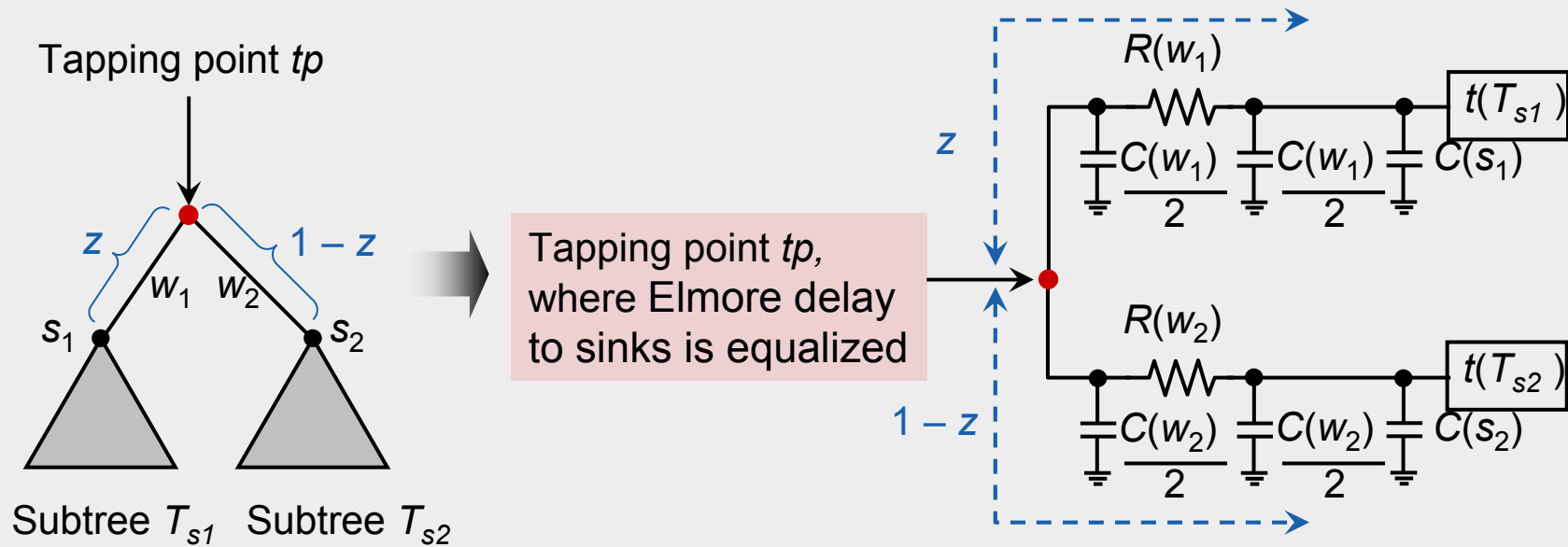
## 7.5.1 Constructing Trees with Zero Global Skew

### Exact Zero Skew

- Adopts a bottom-up process of matching subtree roots and merging the corresponding subtrees, similar to RGM
- Two important improvements:
  - Finds exact zero-skew tapping points with respect to the Elmore delay model rather than the linear delay model
  - Maintains exact delay balance even when two subtrees with very different source-sink delays are matched (by wire elongation)

## 7.5.1 Constructing Trees with Zero Global Skew

### Exact Zero Skew



## 7.5.1 Constructing Trees with Zero Global Skew

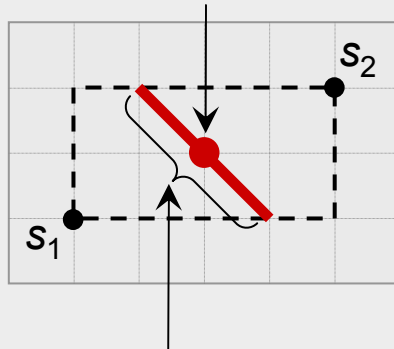
### Deferred-Merge Embedding (DME)

- Defers the choice of merging (tapping) points for subtrees of the clock tree
- Needs a tree topology as input
- Weakness in earlier algorithms:
  - Determine locations of internal nodes of the clock tree too early; once a centroid is found, it is never changed
- Basic idea:
  - Two sinks in general position will have an infinite number of midpoints, creating a tilted line segment – Manhattan arc
  - Manhattan arc: same minimum wirelength and exact zero skew
  - Selection of embedding points for internal nodes on Manhattan arc will be delayed for as long as possible

## 7.5.1 Constructing Trees with Zero Global Skew

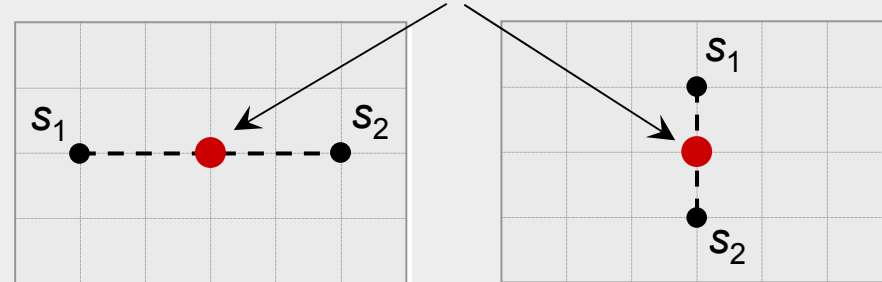
### Deferred-Merge Embedding (DME)

Euclidean midpoint



Locus of all Manhattan midpoints is a **Manhattan arc** in the Manhattan geometry

Euclidean midpoint



Sinks are aligned, hence, **Manhattan arc** has zero length

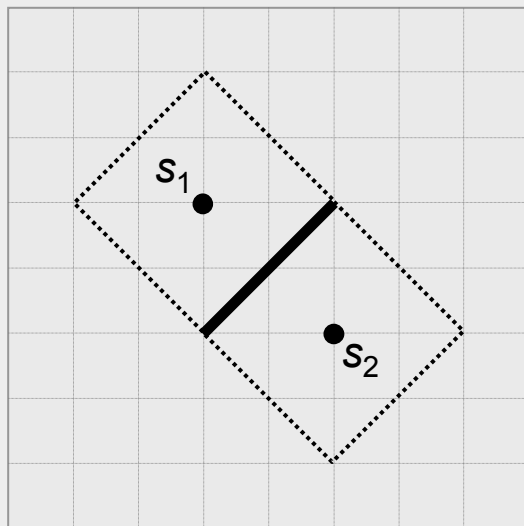
## 7.5.1 Constructing Trees with Zero Global Skew

### Deferred-Merge Embedding (DME)

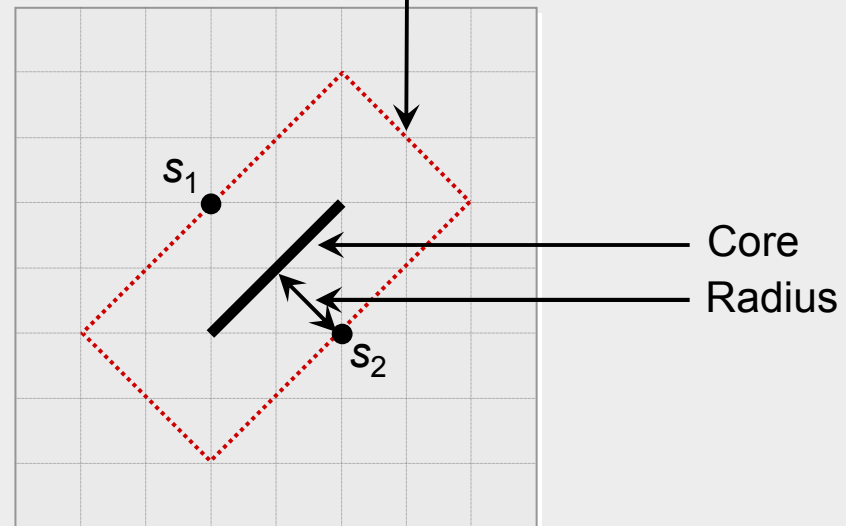
- Embeds internal nodes of the given topology  $G$  via a two-phase process
- **First phase is bottom-up**
  - Determines all possible locations of internal nodes of  $G$  consistent with a minimum-cost ZST  $T$
  - Output: “tree of line segments”, with each line segment being the locus of possible placements of an internal node of  $T$
- **Second phase is top-down**
  - Chooses the exact locations of all internal nodes in  $T$
  - Output: fully embedded, minimum-cost ZST with topology  $G$

## 7.5.1 Constructing Trees with Zero Global Skew

### Deferred-Merge Embedding (DME)

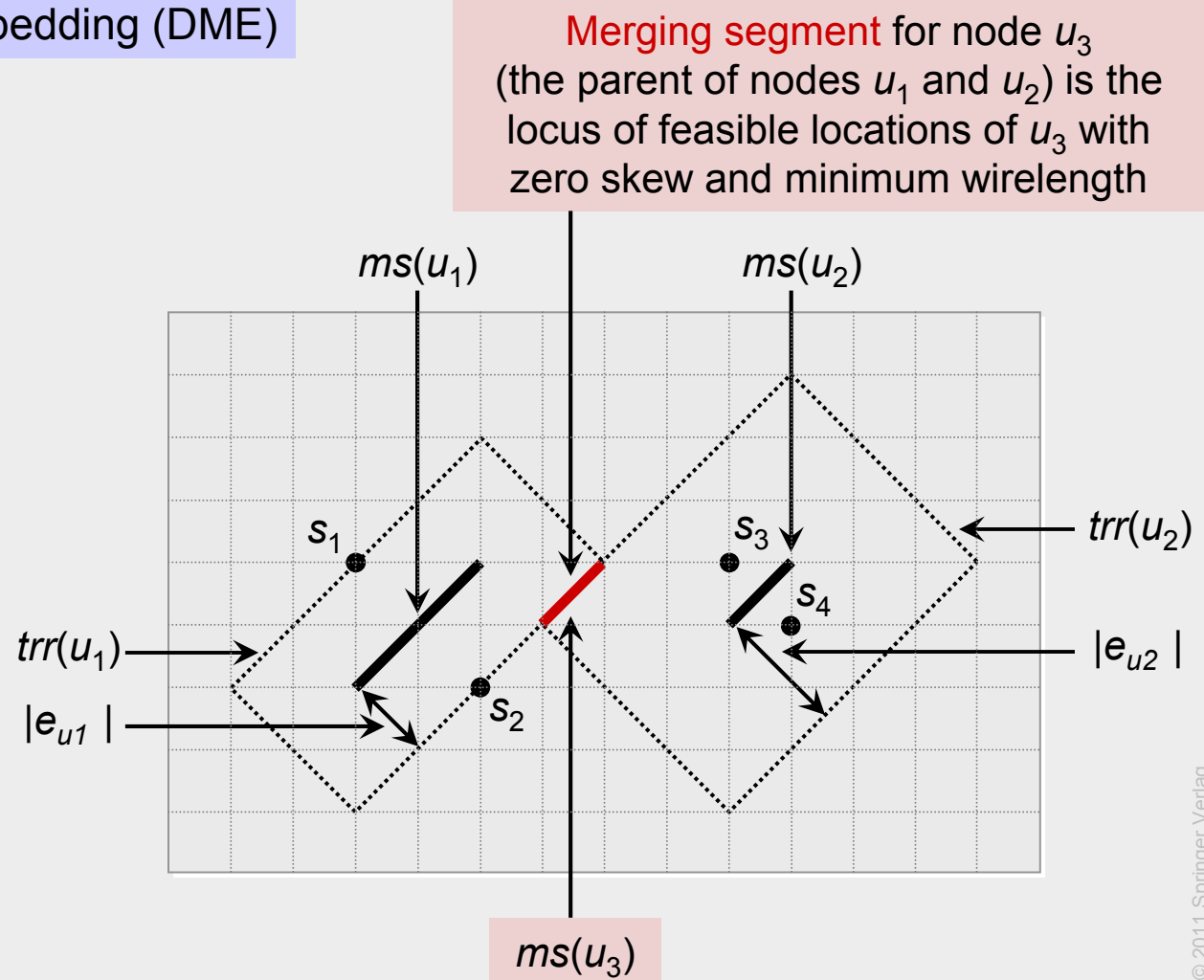
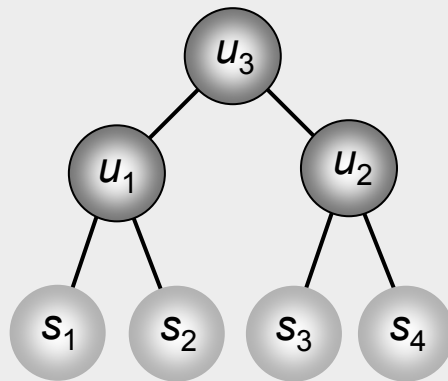


Tilted Rectangular Region (TRR)  
for the Manhattan arc of  $s_1$  and  $s_2$   
with a radius of two units



## 7.5.1 Constructing Trees with Zero Global Skew

### Deferred-Merge Embedding (DME)





## 7.5.1 Constructing Trees with Zero Global Skew

### Deferred-Merge Embedding (DME)

#### Build Tree of Segments Algorithm (DME Bottom-Up Phase)

**Input:** set of sinks  $S$  and tree topology  $G(S, Top)$

**Output:** merging segments  $ms(v)$  and edge lengths  $|e_v|$ ,  $v \in G$

**if foreach** (node  $v \in G$ , in bottom-up order)

**if** ( $v$  is a sink node)

$ms[v] = PL(v)$

**else**

$(a, b) = CHILDREN(v)$

$CALC\_EDGE\_LENGTH(e_a, e_b)$

$trr[a][core] = MS(a)$

$trr[a][radius] = |e_a|$

$trr[b][core] = MS(b)$

$trr[b][radius] = |e_b|$

$ms[v] = trr[a] \cap trr[b]$

// if  $v$  is a terminal, then  $ms(v)$  is a

// zero-length Manhattan arc

// otherwise, if  $v$  is an internal node,

// find  $v$ 's children and

// calculate the edge length

// create  $trr(a)$  – find merging segment

// and radius of  $a$

// create  $trr(b)$  – find merging segment

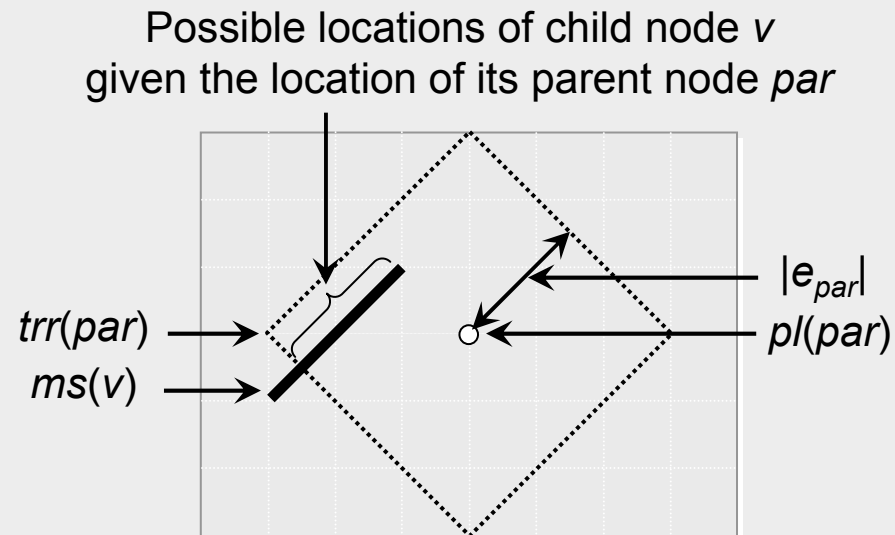
// and radius of  $b$

// merging segment of  $v$

## 7.5.1 Constructing Trees with Zero Global Skew

### Deferred-Merge Embedding (DME)

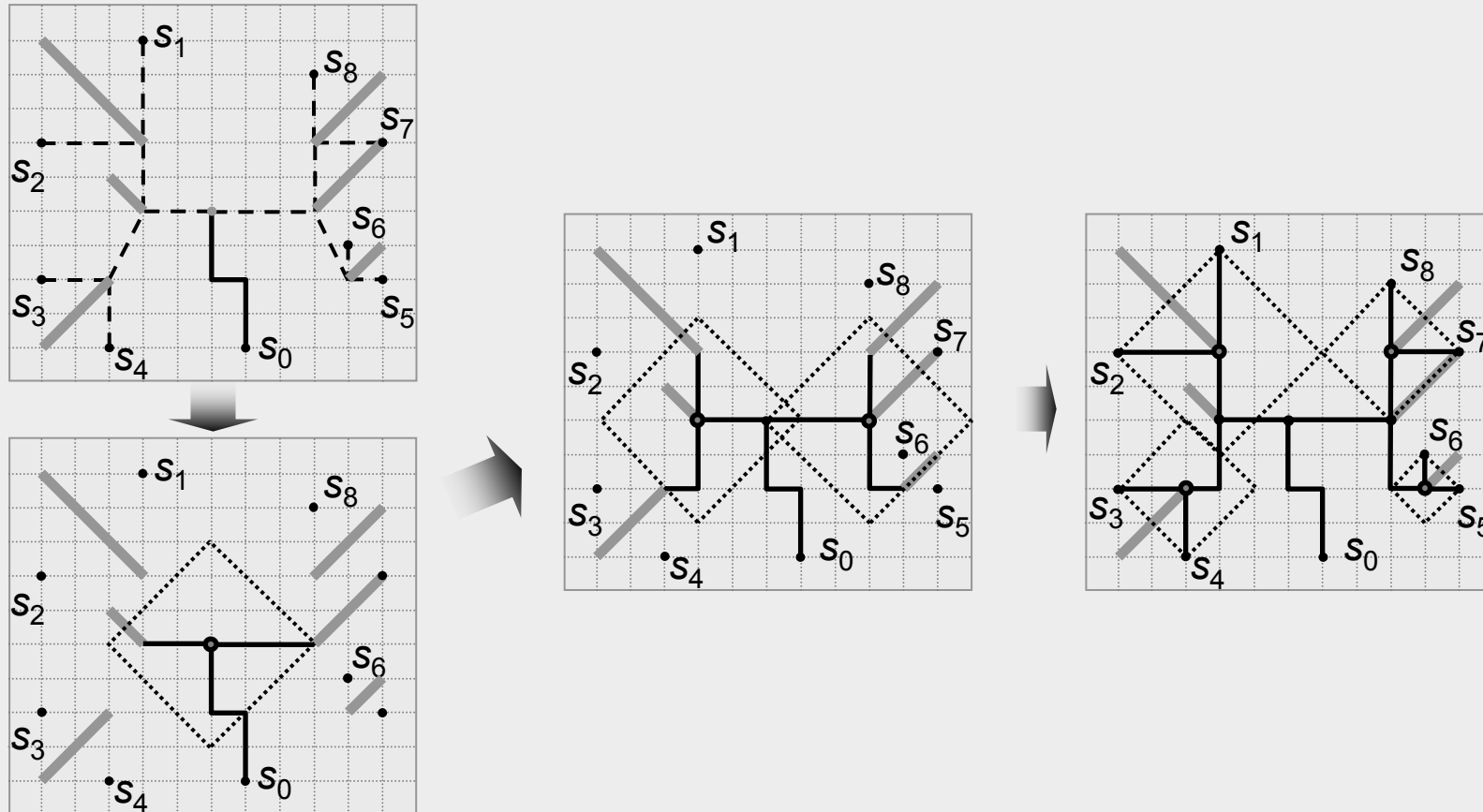
#### Find Exact Locations (DME Top-Down Phase)



## 7.5.1 Constructing Trees with Zero Global Skew

### Deferred-Merge Embedding (DME)

#### Find Exact Locations (DME Top-Down Phase)



## 7.5.1 Constructing Trees with Zero Global Skew

### Deferred-Merge Embedding (DME)

#### Find Exact Locations (DME Top-Down Phase)

**Input:** set of sinks  $S$ , tree topology  $G$ , outputs of DME bottom-up phase

**Output:** minimum-cost zero-skew tree  $T$  with topology  $G$

**foreach** (non-sink node  $v \in G$  top-down order)

**if** ( $v$  is the root)

$loc = \text{any point in } ms(v)$

**else**

$par = \text{PARENT}(v)$

    //  $par$  is the parent of  $v$

$trr[par][core] = PL(par)$

    // create  $trr(par)$  – find merging segment

$trr[par][radius] = |e_v|$

    // and radius of  $par$

$loc = \text{any point in } ms[v] \cap trr[par]$

$pl[v] = loc$

## 7.5.2 Clock Tree Buffering in the Presence of Variation

- To address challenging skew constraints, a clock tree undergoes several optimization steps, including
  - Geometric clock tree construction
  - Initial clock buffer insertion
  - Clock buffer sizing
  - Wire sizing
  - Wire snaking
- In the presence of process, voltage, and temperature variations, such optimizations require modeling the impact of variations
  - Variation model encapsulates the different parameters, such as width and thickness, of each library element as well-defined random variables

## Summary of Chapter 7 – Area Routing

- Area routing: avoiding the division into global and detailed routing
  - Doing everything at once, subject to design rules
  - Small netlists with complicated constraints
  - Analog, MCM and PCB routing
- Manhattan vs Euclidean paths
  - Euclidean paths are no longer than Manhattan, usually shorter
  - Unique Euclidean shortest path
  - Multiple Manhattan paths
  - When Euclidean shortest paths intersect, there may exist Manhattan shortest paths that do not (not vice versa)
- Net ordering is important in area routing
  - Rule 1: nets with higher aspect ratio (less flexible) routed first
  - Rule 2: nets surrounded by other nets (more constrained) routed first
  - Rule 3: nets with more pins inside other net's bounding boxes routed first

## Summary of Chapter 7 – Non-Manhattan Tree Routing

- Recall that Manhattan routing is dictated by the limitations of modern semiconductor manufacturing for thin wires
- PCB routing is not subject to those limitations
  - Can use shorter connections
- Non-Manhattan connections
  - Diagonal (45- or 60-degree) segments in addition to horizontal and vertical segments
  - Create more freedom to place Steiner points
- Octilinear Steiner Tree construction
  - Algorithms are generally adapted from the Manhattan case
  - Should produce results that are at least as good as the Manhattan case

## Summary of Chapter 7 – Clock Network Routing

- Similar to signal-net routing, except for
  - Very large numbers of sinks
  - The need to equalize propagation delays from the root to sinks
  - Longer routes (to satisfy the equalization constraint)
  - Typical algorithms determine topology first, then geometric embedding
- Clock skew
  - Consider propagation delay from the root to each sink
  - Skew is the maximal pairwise difference between delays (over all pairs of sinks)
  - May be limited to sinks that are within distance  $d > 0$  (local skew)
- For a specified wire delay model
  - ZST: Zero-Skew Tree routing requires that skew = 0
  - BST: Bounded-Skew Tree routing requires that skew < *Bound*

## Summary of Chapter 7 – Modern Clock Tree Synthesis

- Initial clock tree construction
  - Topology determination (MMM or RGM)
  - DME embedding (different flavors for ZST and BST)
  - Working with the Elmore delay model requires more effort than working with linear delay models
- Geometric obstacles (e.g., macros)
  - May require detours
  - Can be handled during DME (complicated) or during post-processing (often achieves as good results)
- Clock-tree optimization
  - Buffer insertion
  - Buffer sizing
  - Wire sizing
  - Wire snaking by small amounts
  - Decreasing the impact of process variability